Gyroscopic waves in the Mediterranean Sea

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1. Introduction

[1] In the ocean outside areas of dense-water formation, coherent vertical motions (w) are generally much weaker (≈10⁻³) than horizontal (u, v) ones. According to theoretical models based upon “the traditional approximation”, i.e. where the horizontal component of the Coriolis force is neglected, describing inertio-gravity waves in the ocean interior, this holds especially for motions at the inertial frequency f: w(f) < O(10⁻³). We present observations of significant w(f), with mean values of 10⁻²(u(f),v(f)) and occasional values of 1(u(f),v(f)), from the deep Western Mediterranean Sea characterized by very small buoyancy frequency N = 0 ± 0.4f. Our observations also present evidence of vertical propagation of internal waves, originated in the near-surface density stratified layers, through homogeneous layers below. The observations could be interpreted only within the framework of “non-traditional approach” with the horizontal component of the Coriolis force fully taken into account. Citation: van Haren, H., and C. Millot (2005), Gyroscopic waves in the Mediterranean Sea, Geophys. Res. Lett., 32, L24614, doi:10.1029/2005GL023915.

2. Inertio-Gravity Waves

[2] Inertial motions are amongst the most energetic motions in large parts of the ocean, with magnitudes comparable to those of tidal currents. Vertical differences in horizontal inertial motions, inertial shear, generally dominate tidal shear due to a smaller vertical length scale linked to the vertical stratification in density. As a result, inertial motions are important for deep-ocean mixing. As stratification can support internal (inertio-)gravity waves, commonly used theories based on the traditional approximation predict propagating waves at super-inertial frequencies. At f, pure oscillations can exist that do not propagate but are rapidly damped by (bottom) friction. For weakly stratified waters, the non-traditional approach, considering the horizontal component of the Earth’s rotational vector, predicts (also vertically) propagating inertio-gravity waves (or gyroscopic waves in homogeneous water), besides at sub-inertial frequencies, also at f [LeBlond and Mysak, 1978; Gerkema and Shrira, 2005]. Although such waves are characterised by relatively large w(f) values O(10⁻¹⁻¹–1–1(u(f), v(f))), they have never been observed in situ up to now. Here we show such w(f) values in recent acoustic Doppler current profiler (ADCP) observations from a deep layer that is nearly-homogeneous as far as can be measured by today’s instruments.

[3] Inertial motions are mainly generated near the surface by temporal variability in wind stress, due to the Coriolis effect of the rotating Earth [e.g., Webster, 1968; Perkins, 1972; Millot and Crépon, 1981; Garrett, 2001]. However, enhanced near-inertial energy can be found in the deep [Fu, 1981; Saunders, 1983; van Haren et al., 2002], suggesting possible generation near the bottom due to relaxation of fronts as hypothesised for surface waters [Tandon and Garrett, 1995], downward energy propagation via fronts [Davies and Xing, 2004] or accumulation of canonical (GM [Garrett and Munk, 1972]) internal waves encountering their turning latitude [Fu, 1981]. In the absence of (relaxing) fronts, the latter model may explain a 7 dB elevation of near-inertial energy above the background spectral level for a mid-latitude ocean, but it cannot explain the observations presented here because i) the observed near-inertial spectral peak is 13–20 dB above the background level, ii) the Western Mediterranean Sea extends only ∼600 km in meridian direction (equivalent to ±6% variation in f), which is a very small portion of the GM spectrum, and iii) the downward propagating motions have to pass substantial layers (100 m) of truly neutral stability that do not support internal gravity waves [van Haren and Millot, 2004]. Hence, local near-surface generation is more likely [Fu, 1981], which is plausible given the strong pulse-like winds from the north that generate near-surface inertial motions in the whole sea [Millot and Crépon, 1981], and we hypothesise deep-sea propagation through homogeneous and well-stratified layers using the non-traditional approach, focusing on gyroscopic waves.

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following (1) no possibility exists for a transfer between sub- and super-inertial motions (e.g. across an interface separating homogeneous and stratified waters). As in the deep ocean N can become so small that it approaches f, a complete reflection is predicted of free inertial waves generated near the surface encountering layers where N = f [Munk, 1981].

[5] In contrast, the non-traditional approach [Saint-Guily, 1970; LeBlond and Mysak, 1978; Gerkema and Shrira, 2005] takes into account $f_0 = 2\Omega \cos \varphi$ and the complete set of linear terms in momentum equations. This results in the extension of the range [f, N] to $[\sigma_{\min} < f, \sigma_{\max} > N]$, with the smallest scale motions at $\sigma_{\min}$ (trapping). For $N = 0$, the wave band is in the range [0, 2f]. As $f < 2\Omega$, inertial motions can thus propagate as free waves in homogeneous waters. Under an f-plane approximation the non-traditional inertial wave propagation is described for every N by [Badulin et al., 1991; Gerkema and Shrira, 2005]:

$$dz = \frac{f_0^2 (f^2 + (\sigma^2 - f^2) (N^2 - \sigma^2 + f^2))^{1/2}}{N^2 - \sigma^2 + f^2},$$

(2)

where $f_0 = f \sin \alpha$. The two solutions in (2) (or $\xi$) can have very different slopes, whilst the two solutions in (1) are identical. This holds for any $\alpha$, except for waves propagating in the East-West ($x$, zonal, $\alpha = 0$, $\pi$) direction or for large N $> f$ for which (2) approaches (1).

[6] From (1) one can expect vertically steep f-energy propagation and thus a large ratio $|w(f)|/|u(\Omega)|, |v(f)|$ (as well as $w(f) = 0$, with large $u, v$, due to horizontal slopes for the second solution!) for waves propagating in North-South ($y$, meridian, $\alpha = \pi/2$, $3\pi/2$) direction, also in weak stratification (N $\approx 0 < f$).

[7] As the particle motion of f-waves are always circular in their plane of energy propagation and as this plane varies its angle to the vertical depending on N and $\alpha$ (and $\varphi$), horizontal f-motions describe a clockwise-polarised ellipse having a polarization expressed as an eccentricity (E) ranging between near-circular (E = 1) and near-rectilinear (E = 0) when projected on the $x, y$ plane [van Haren and Millot, 2004] (the two extremes are found for meridian propagation). Energy propagation is in the direction of the minor axis. When the horizontal current describes a nearly rectilinear ellipse at f, a relatively large vertical current w(f) is expected, which does not exist in traditional theory.

[8] So far, gyroscopic waves were only observed in the laboratory [Oser, 1958; McEwan, 1970; Manders and Maas, 2003]. Recently, van Haren and Millot [2004] extensively described ellipse properties of near-inertial horizontal current meter observations. These ellipse properties varied strongly with time and across the vertical in the Western Mediterranean Sea (vertical currents were not available). These variations suggested a smooth transition of inertia-gravity waves through layers where N changed from near-zero to a non-zero value $> f$. To provide further evidence of the above, we deployed at the same site a four-beam 75 kHz ADCP to investigate w(f) and vertical propagation of phase, which is opposed to energy propagation in the vertical for N > f but, due to a sign change in the denominator in (2), identical (up or down) for N = 0 when $\alpha < \sin(\tan(\varphi))$, $\approx 53^\circ$ in our area.

3. Data and Background Conditions

[9] The upward-looking ADCP was moored (together with a thermistor string that did not function correctly) to the southwest of Sardinia in the Algerian sub-basin of the Western Mediterranean Sea (Table 1). The ADCP was set in a 400 kg net buoyancy elliptical float at a depth of $\sim 2400$ m, because it was expected to range $\sim 500$ m and because the upper limit of the deep homogeneous layer was previously found at $\sim 2200$ m (from CTD observations in 1997 and 2001).

[10] Unfortunately, only a range of 200–250 m of permanently good data was realized, due to low amounts of scatterers. In addition, the homogeneous layer, which corresponds to a water mass formed in the north of the Western Mediterranean Sea in winter, was thicker than expected during at least part of the experiment. Its upper limit was at $\sim 1900$ m in September 2004 (Figure 1, upper right panel). Using a Sea-Bird SBE 911 plus CTD, sampling at 24 Hz temperature accurate to within 10$^{-3}$ °C and conductivity to within 3·10$^{-4}$ S m$^{-1}$, we estimated N = 0 within an uncertainty of 0.4f in the layer below 1900 m. This uncertainty was $\sim$ half due to instrumental errors and $\sim$ half due to the imperfect estimation of the adiabatic lapse rate. Although the circulation of this (nearly) homogeneous water was known to be significant [Millot, 1999], such a variation in its upper limit was not expected. The $\sim 1900$ m limit corresponds to the depth of the channel of Sardinia so that dense water “in excess” in the Algerian sub-basin is expected to outflow into the Tyrrhenian sub-basin (the 2004 situation). A limit at $\sim 2200$ m (the 1997 and 2001 situations) is indicative of a dense water “deficit”. Above the deep layer of N = 0, a $\sim 500$-m thick layer of very constant stratification (N = 2.5 ± 0.5f) is found during both the former and the recent experiments. Although the limit between the two layers varied with time, we expect the 200–250 m range of the ADCP mostly in the homogeneous layer (which is supported by the similarity of the currents over the vertical).

[11] The large buoyancy caused very little mooring motion, as evidenced from pressure and tilt sensor information: variations were <2 m in the vertical or <2.5° tilt angle. The thermistor string did not affect the ADCP’s current...
measurements, as was verified by inspecting the acoustic backscatter records, confirming previous [Schott, 1988] experiments with a similar thermistor string mounted in a 75 kHz ADCP beam. As a result, good quality w-data were expected to an accuracy of $3 \times 10^{-4}$ m s$^{-1}$ at f, as the inertial period is $\sim 80$ times the ensemble period (for which error is given in Table 1). This quality was further verified using the additional ‘error velocity (err)’ parameter, defined [RD Instruments, 1999] as the difference between two estimates of w computed from the two beam pairs and multiplied by a proper scaling factor [van Haren et al., 1994] for comparison with w. Horizontal and vertical current inhomogeneity, for example caused by an object obstructing one or more beams, affect vertical current measurements when err $\rightarrow$ w. However, w(f) is significantly measured here because $|w(f)|^2 > 10|\text{err}(f)|^2$ as observed below 2200 m (Figure 1, upper left panel), and the main source of the small error in w(f) is instrumental noise.

4. Observations

[12] Inertial kinetic energy $P_{\text{KE}}(f)$ dominates spectra (Figure 1 upper left panel) even though $N = 0 \pm 0.4f < f$ (Figure 1 upper right panel). The peak at f has a finite width, which yields the familiar intermittency [Fu, 1981] visible in the depth-time plots of band-pass filtered near-inertial motions (Figure 1 middle panels; v gives a similar picture as u). Bands of large f-current amplitude extend vertically across most of the 480-m range, despite the often bad return above $\sim 2200$ m. Note that the intermittency of near-inertial u (or v) and w vary quasi-independently, so that they sometimes show simultaneous large (or small) amplitudes and sometimes opposing in(de)creases in amplitude. As a result, the ratio $|w(f)|/|u(f)|$ varies strongly with time. This variability cannot be attributed to motions forced by bottom slopes, which would yield w in(de)creasing with u or a constant amplitude ratio, besides a relatively low one of $\sim 0.05$ (the average bottom slope towards Sardinia). The observed variability is a property of inertia-gravity waves since the two solutions of (2) are very different and any variations in f-motions’ source may result in a different response, due to dependence of $N, \alpha$.

[13] The detail depth-time plot of u(f) (Figure 1 lowest panel) shows downward propagation of phase. For $N = 0$, $\alpha < 53^\circ$ this implies downward energy propagation. The weak vertical slanting of $45 \pm 45^\circ/300$ m points at relatively large vertical phase speeds of $\sim 2400 \pm 2400$ m/inertial period. Downward phase propagation occurred most of the time (>90%), but the slope varied. However, most conspicuous are the w-observations: w is non-zero with a peak at f (Figure 1). Such a peak is absent in the error velocity (‘err’) spectrum, which represents white noise. In

Figure 1. Upper left panel shows spectra in $10^{-4}$ m$^2$ s$^{-2}$/cpd i at 2370 m: kinetic energy (KE; black), vertical velocity$^2$ (w; dark-blue) and error velocity$^2$ (err; green), ii) horizontal current difference$^2$ between 2210 and 2370 m (AU; red), iii) vertical velocity$^2$ (w; light-blue) at 2180 m (representing the upper range of good data). Upper right panel shows the density anomaly profile (referenced to 2000 m) obtained in September 2004. The ADCP range is given to the left, with continuous good data in green. The purple lines indicate density stratification yielding $N = 0$, $2f$ (solid lines) and $N = f$, $3f$ (dashed lines). The two middle panels show the entire depth-time series of near-inertial ADCP-data (band-pass filtered between 0.9–1.1f) for w (multiplied by 10) and u, using the same colors, which are specified in the lowest panel. The horizontal bars indicate the detail period shown in the lower two panels, in which the inertial periodicity is visible (a maximum every 19.3 h). The horizontal white line indicates the approximate depth below which in general good data were obtained.
the good-data range, err(f) is at least one order of magnitude less energetic than w(f) and equal to the manufacturer’s error estimate, which is also found in w for α > 10 cpd. Thus, the observed w(f) are significant within the 95% level. In the overall mean the ratio |w(f)/u(f)| = 0.12 ± 0.05, with periods when w approaches u (Figure 1 middle panels). [14] This variation with time is clearly seen in the detail example in Figure 1. Between days 286—294 |w(f)/u(f)| → 1 is found for depths between 2050—2200 m, whilst the ratio approaches the overall mean value towards day 298. Below 2200 m the mean |w(f)/u(f)| = 0.35 ± 0.1 for this 14 days period. These values, including the overall mean of 0.12, are all far too large to be explained using the traditional approximation. A ratio of |w(f)/u(f)| > 0.35 implies a (19° to the vertical) inclined circular motion that is observed as a horizontal current with E ≈ 0.94 (the mean value observed at ∼2350 m), whilst |w(f)/u(f)| = 1.0 (inclination of 45°) gives E ≈ 0.7 (the mean value observed at ∼2200 m). These E(f) conform to (2) for near-inertial gyroscopic waves (N = 0) when the propagation is nearly zonal (α ≈ 8, 19 (+180°), respectively), as was observed. Variability in E has further been demonstrated in hodographs in [van Haren and Millot, 2004]. E’s variability with depth and time, like that of |w(f)/u(f)|, reflects local variations in relative importance of the two solutions in (2), as a function of variations in near-inertial sources in the layers above and as a function of frontal variability.

5. Discussion

[15] We hypothesize that near-inertial inertia-gravity waves were generated near the surface, as propagation was downward, and in the detailed example in Figure 1 more or less east-west (α ≈ 8° < 53°). Then we expect from (2) in the layer N = 2.5f |w(f)/u(f)| ≈ 0.07, instead of 0 expected from (1), down to 1900 m, compared to 0.36 observed (in N = 0). Unfortunately, the above change in values is not observed. In the near-homogeneous layer energy sometimes increases towards the bottom, evidence of gyroscopic wave trapping, as suggested theoretically [Gerkema and Shrira, 2005], but certainly not decreasing exponentially as expected for gravity ‘waves’ [Munk, 1981].

[16] As near-inertial gyroscopic waves have propagation directions that markedly differ from those of internal gravity waves, we expect distinctly different properties of vertical transport (due to the possibility of much larger w) and deep-ocean mixing (due to their shear magnitude that much more rapidly varies with time). Details of the suggested transfer between stratified and homogeneous layers are yet to be verified. However, observational evidence is given here of near-inertial gyroscopic waves, i.e. internal waves in truly homogeneous water N = 0, estimated better than 0.4 f, that have not been observed in the ocean before. The observed mean ratio w/f is of the same order as found for sub-inertial motions in restricted areas of deep-water formation [Voorhis and Webb, 1970; Gascard, 1973], but here the motions are at f so that we deal with |w(f)/u(f)| ≈ 0.1.

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